

# Micro Meritics

## Unit - IV

It is the study of the fundamental and derived properties of individual as well as collection of particles.

Particle size -

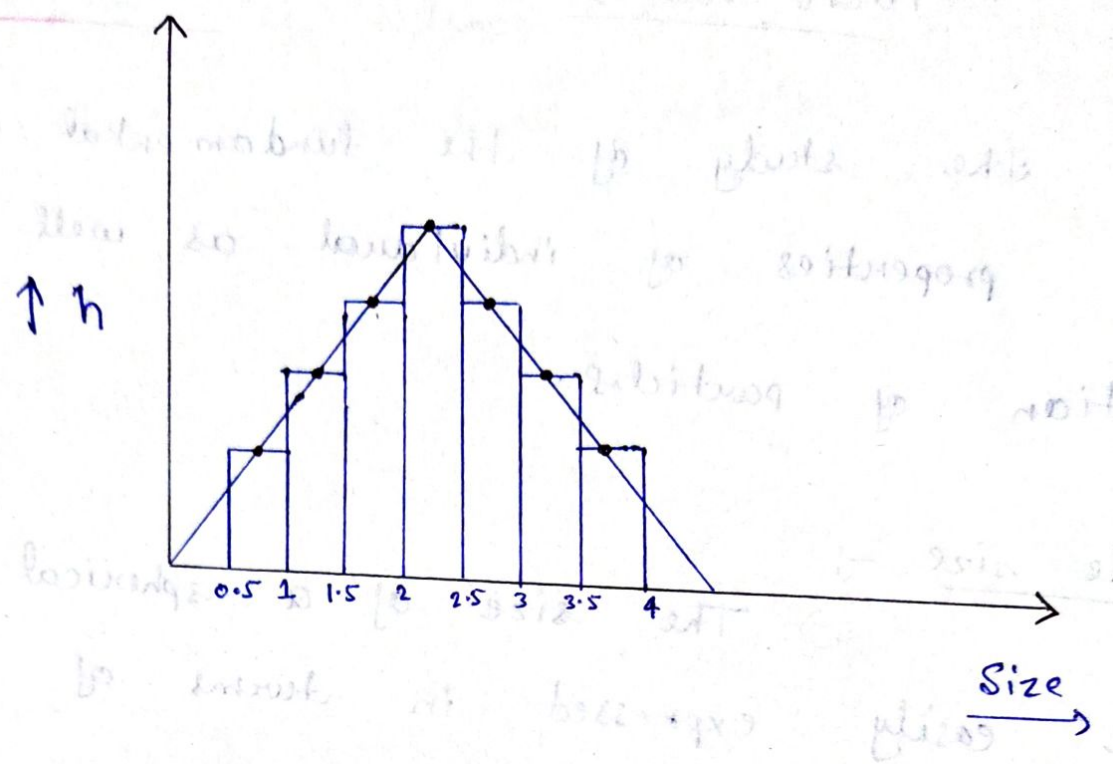
The size of a spherical particle can be easily expressed in terms of its diameter.

\* The average particle size of powder may be calculated by —

$$\text{Average particle size} = \frac{\sum id}{\sum n}$$

S.N.	Size range ( $\mu\text{m}$ )	mean size range ( $\mu\text{m}$ )	no. of particle (n)	hd
1	0.5-1	0.75	94	3
2	1-1.5	1.25	18	22.5
3	1.5-2	1.75	33	68.25
4	2-2.5	2.25	73	164.25
5	2.5-3	2.75	24	66
6	3-3.5	3.25	14	45.5
7	3.5-4	3.75	02	7.5

VI - list



(a) For a perfect sphere —

$$\text{Surface area } (S) = \pi d^2$$

$$\text{Volume } (V) = \frac{\pi d^3}{6}$$

(b) For a non-spherical particle → Particle size can be calculated in terms of equivalent spherical diameter.

That is surface area, volume, diameter, projected diameter and Stokes diameter.

2.85	11	2.1	3.1
2.5-2.8	20	3.1-1	3.1-1
2.2-2.5	3.7	2.5-2	2.5-2
2.0	4.5	2.5-2	2.5-2
2.2-2.0	11	2.5-2	2.5-2
2.0	11	2.5-2	2.5-2

## Particle size distribution -

A collection of particles having mixture of varying size and shape, the number of particle of same size range present in a sample is size distribution.

\* Particle size distribution can be calculated by following two ways -

① By determining number of particles present in each size range (microscopy technique).

② By determining weight of particle present in each size range (sedimentation and sieving method).

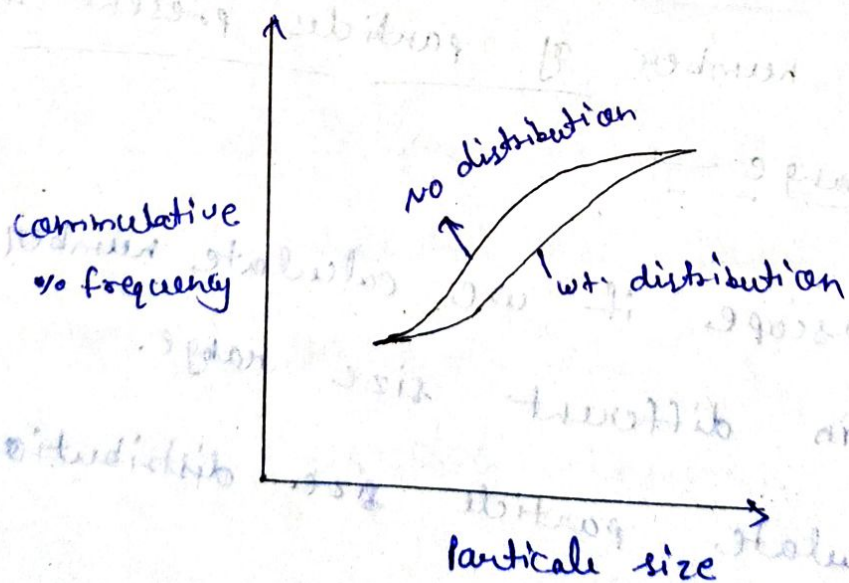
① By determining number of particles present in each size range -

\* By using microscope if we calculate number of particle in different size range.

\* We can calculate particle size distribution by using table below -

S.N.	Size range (μm)	Mean size (d) range (μm)	No. of particle frequency (n)	% f	Frequency cumulative
1	0.5-1	0.75	04		
2	1-1.5	1.25	18		
3	1.5-2	1.75	39		
4	2-2.5	2.25	73		
5	2.5-3	2.75	24		
6	3-3.5	3.25	14		
7	3.5-4	3.75	02		

When the number of particles is plotted against the mean particle size, the curve obtained is called number frequency distribution curve.



⑪ By determining weight of particle present in each size range (sedimentation and sieving) -

- \* To determine weight of particle present in each size range, we can use sieving method.
- \* In this method we can arrange sieve according to the descending order of their pore size.
- \* After shaking sieve for sufficient time.
- \* The particle settle of sieve according to their size.
- \* By weighing particle on sieve, we can obtain weight of particle according to their size.

Seive no.	Pore size	Frequency wt. (gm)	% F	cumulative % F

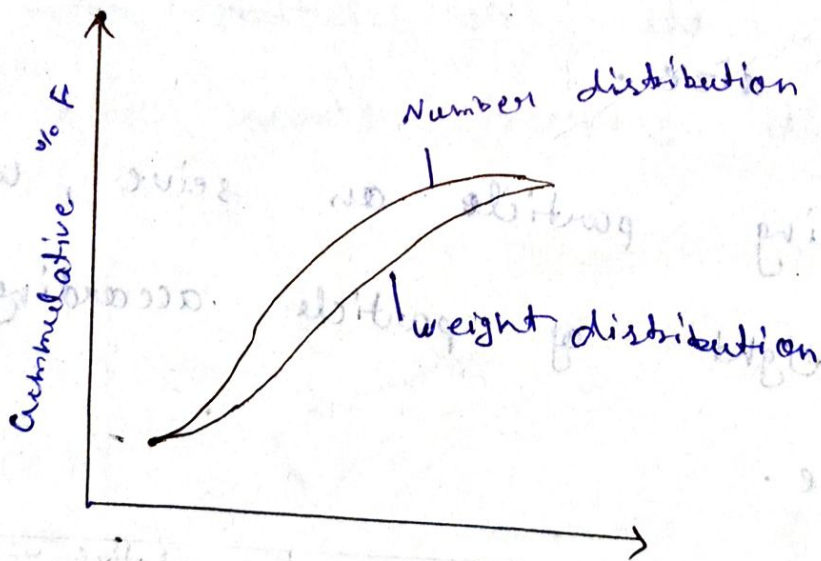
When the weight of particle is plotted against mean particle size, the curve obtained is known as weight distribution curve.

$$\% \text{ Frequency} = \frac{\text{weight obtained}}{\text{Total weight}} \times 100$$

Cumulative % Frequency = (i) 1%

(ii) 1% + 2%

(iii) 1% + 2% + 3% + 7%



particle size			

## Particle number

The particle number is defined as the number of particles per unit weight of a powder. It can be obtained by —

$$N = \frac{\text{1 gm of powder}}{\text{mass of one particle}}$$

where —

$$\text{Volume of single particle} = \frac{\pi d^3}{6}$$

$$\therefore \text{density} = \frac{\text{mass}}{\text{Volume}}$$

$$\therefore \text{mass} = \text{Volume} \times \text{density}$$

$$\text{mass} = \frac{\pi d^3 \rho}{6}$$

$$N = \frac{1 \times 6}{\pi d^3 \rho}$$

Q-1 → If mean volume number diameter of a sample powder is 3.62  $\mu\text{m}$ .

If the density of the powder is 3  $\text{gm/cm}^3$ , what is the number of particle per gram.

$$N = \frac{6}{\pi d^3 \rho}$$

$$N = \frac{6}{2}$$

$$3.14 \times 3.62 \times 3.62 \times 3.62 \times 10^{-12}$$

$$N = \frac{2 \times 10^{12}}{3.14 \times 3.62 \times 3.62 \times 3.62}$$

$$N = \frac{200 \times 10^{10}}{47.93 \times 3.14}$$

$$N = \frac{200 \times 10^{10}}{149}$$

$$N = 1.34 \times 10^{10}$$

$$N = \frac{2 \times 10^{12}}{149}$$



## Particle size determination

The following methods are generally used for the determination of particle size and particle size distribution.

### 1- Microscopic technique ->

This technique can be used for particle size in the range  $0.2 \mu\text{m} - 100 \mu\text{m}$ .

- \* A dilute suspension of the particles is prepared in the liquid in which it is insoluble.
- \* A drop of suspension is mounted on a slide and observed under the microscope.
- \* The eye piece of the microscope is fitted with a micrometer.
- \* All particles observed in the field are counted through eye piece.
- \* The data may be scientifically represented as size frequency distribution curve.
- \* The average particle size and size distribution

is determine.

\* For measuring very small particle an electron microscope or scanning electron microscope may be used.

### Advantages -

\* Agglomerates as well as particles of more than one components can be determined by this method.

### Disadvantages -

\* The measured diameter of the particle represent its dimensions that is length and breadth and an estimate of the depth is not obtained.

Q<sub>1</sub> → The following data was obtained by means of an optical microscope.

<u>Particle size</u>	<u>Number of particles</u> (n)	<u>hd</u>
5	3	15
10	8	80
15	4	60
20	2	40

Calculate the average particle size

$$\text{Avg. size} = \frac{195}{17} = 11.47 \mu\text{m}$$

## 2 → Sieving method (Techniques) :-

\* In this technique the powder whose particle size is to be determined is placed on the sieve placed one another.

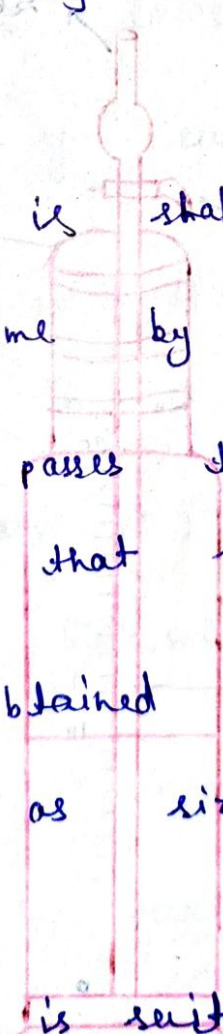
\* The sieve of largest aperture is placed on top followed by sieves of decreasing pore size.

\* The powder is shaken for a definite period of time by mechanical shaker.

\* The powder passes through sieve and retain on that sieve depending upon their size.

\* The data obtained is analyzed and particle size as well as size distribution is calculated.

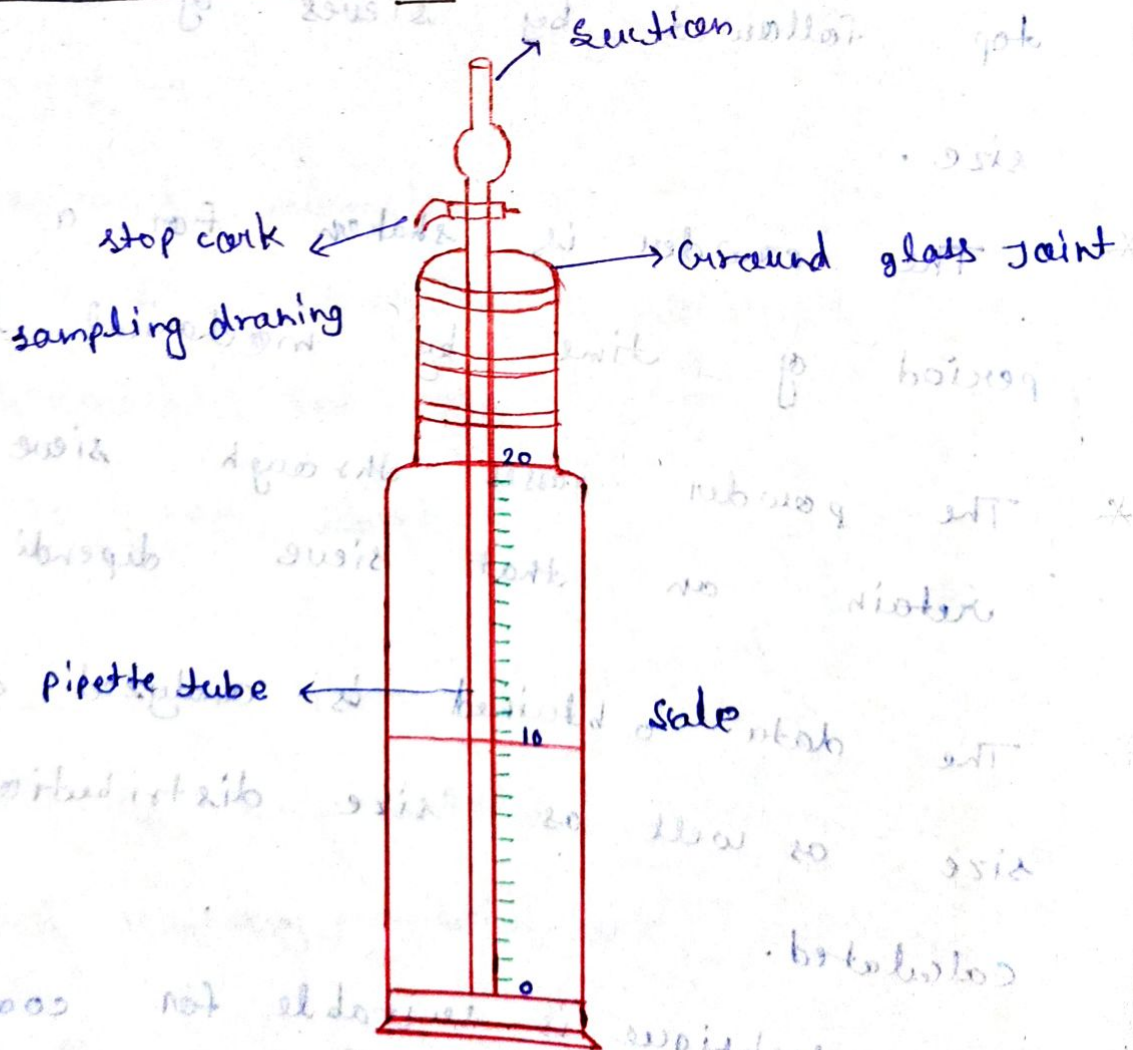
\* This technique is suitable for coarse particle (not less than 50  $\mu\text{m}$ ).



## Disadvantages

- \* Attrition of particles during sieving may lead to size reduction.
- \* Sieve loading and duration of mechanical shaking can influence the result.
- \* Moisture may lead to aggregation of powders.

## 3- Sedimentation techniques -!



Andreasen pipette

- \* This method is used for particle size distribution by sedimentation technique.
- \* The apparatus consist of 550 ml stoppered cylindrical vessel.
- \* The vessel has 5.5 cm. internal diameter and a vertical scale of 0-20 cm. on it.
- \* The stopper has 10 ml bulb pipette and a side tube for sample discharge.
- \* The pipette has lower tip 20 cm. below the surface of suspension.
- \* For analysis, 1-2% suspension of powder is prepared in a medium.
- \* The suspension is introduced into the vessel upto 550 ml mark.
- \* The vessel is stoppered and shaken to distribute the particle.
- \* The pipette is than placed and constant temperature bath.

\* At various time intervals 10 ml sample of suspension are withdrawn.

\* The sample is taken in previously weight china dish.

\* The samples are evaporated and weighed.

\* The particle diameter is calculated by stocks equation —

$$V = \frac{h}{t} = \frac{d_{st}^2 (\rho_s - \rho_0) g}{18 \eta_0}$$

where  $\rightarrow$

$V$  = Rate of settling.

$h$  = distance of fall in time ( $t$ )

$d_{st}$  = mean diameter of particles

$\rho_s$  = Density of particle.

$\rho_0$  = Density of medium.

$g$  = Acceleration due to gravity

$\eta_0$  = Viscosity of medium

\* The weight of each sample is called the weight under size and the sum of successive weight is  $k/\text{os}$  cumulative weight under size.

### Particle shape

\* The particle shape is its geometric shape and surface irregularity, it affects packing property.

\* The shape of particle may be of following types —



Spherical smooth



spherical rough



spherical irregular



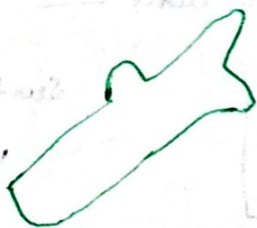
Rounded



Acicular



Angular



Angular



Elongated irregular



Dendritic

- \* A sphere has minimum surface area.
- \* A sphere is categorised by its diameter.
- \* Asymmetric particles have greater surface area.

\* Asymmetric particles surface diameter is measured in terms of equivalent spherical diameter.

\* Equivalent spherical diameter of sphere have same surface area as symmetric particle.

### Specific surface

Specific surface of a powder is defined as the surface area per unit volume ( $S_v$ ) or surface area per unit weight ( $S_w$ ).

\* It may be derived from equation —

① Asymmetric particles —

Surface area per unit volume —

$$S_v = \frac{\text{Surface area}}{\text{Volume}}$$

$$\begin{aligned} \text{Surface area} &= \alpha_s d^2 \\ \text{Volume} &= \alpha_v d^3 \end{aligned}$$

$$S_v = \frac{k \alpha_s d^2}{k \alpha_v d^3} \Rightarrow$$

$$S_v = \frac{\alpha_s}{\alpha_v d} \quad \text{--- ①}$$



Surface area per unit weight —

$$S_w = \frac{\text{Surface area}}{\text{Weight}}$$

$$S_w = \frac{A \rho_s d^2}{A \rho_v d^3 \rho}$$

$\Rightarrow$

$$S_w = \frac{\rho_s}{\rho_v d \rho} \quad \text{--- (1)}$$

(ii) Spherical particle —

Surface area per unit volume —

$$S_v = \frac{A \times d^2 \times 6}{A \times d^3}$$

$$S_v = \frac{6}{d} \quad \text{--- (1)}$$

Surface area per unit weight —

$$S_w = \frac{\text{Surface area}}{\text{Weight}}$$

$$S_w = \frac{A \times d^2 \times 6}{A \times d^3 \rho}$$

$$S_w = \frac{6}{d \rho} \quad \text{--- (ii)}$$

## Method for determining surface area

The surface area can be determined by

one of the following 2 methods —

- ① Adsorption method.
- ② Air permeability method.

### 1 - Adsorption method -

The amount of gas or solute adsorbed on the sample of powder is found out, and the surface area of the powder is determined —



① By using a solute which form a monolayer —

- \* This method involve the adsorption of solute from it's solution on the surface of powder whose area is to be determined.
- \* Firstly a solution of suitable solute is prepared in powder insoluble medium.
- \* A known amount of powder is added in solution.
- \* After equilibrium the powder is filtered and remaining solute is determined.
- \* Difference b/w quantity added and remaining gives the amount adsorbed.
- \* If  $X$  gm. of solute adsorbed.
- \* 1 gm. mole of material contain avogadro's number  $6.0223 \times 10^{23}$  number of molecules.
- \* Total number of molecules will be —

$$X \times 6.0223 \times 10^{23}$$

\* Surface area of 1 molecule of solute is known  
surface area of powder can be calculated.

(ii) By using adsorption of gas on powder —!

\* Quantasorb is an instrument used for determination of surface area by gas adsorption method.

\* The powder whose surface area is to be determined is introduced into a cell.

\* Nitrogen is used as adsorbed gas and helium is an inert gas and passed through the powder in the cell.

\* A thermal conductivity detector measures the amount of nitrogen adsorbed at every equilibrium pressure.

\* A bell shaped curve is obtained on a strip chart recorder.

\* The signal height gives the rate of adsorption of nitrogen gas.

\* The area under curve gives the amount of gas adsorbed on the powder sample.

\* The volume of nitrogen gas  $[C_{Um}]$  in  $cm^3$  adsorbed by 1 gm. of powder is given by BET equation

$$\frac{P}{V(P_0 - P)} = \frac{1}{V_m b} + \frac{(b-1)P}{V_m b P_0}$$

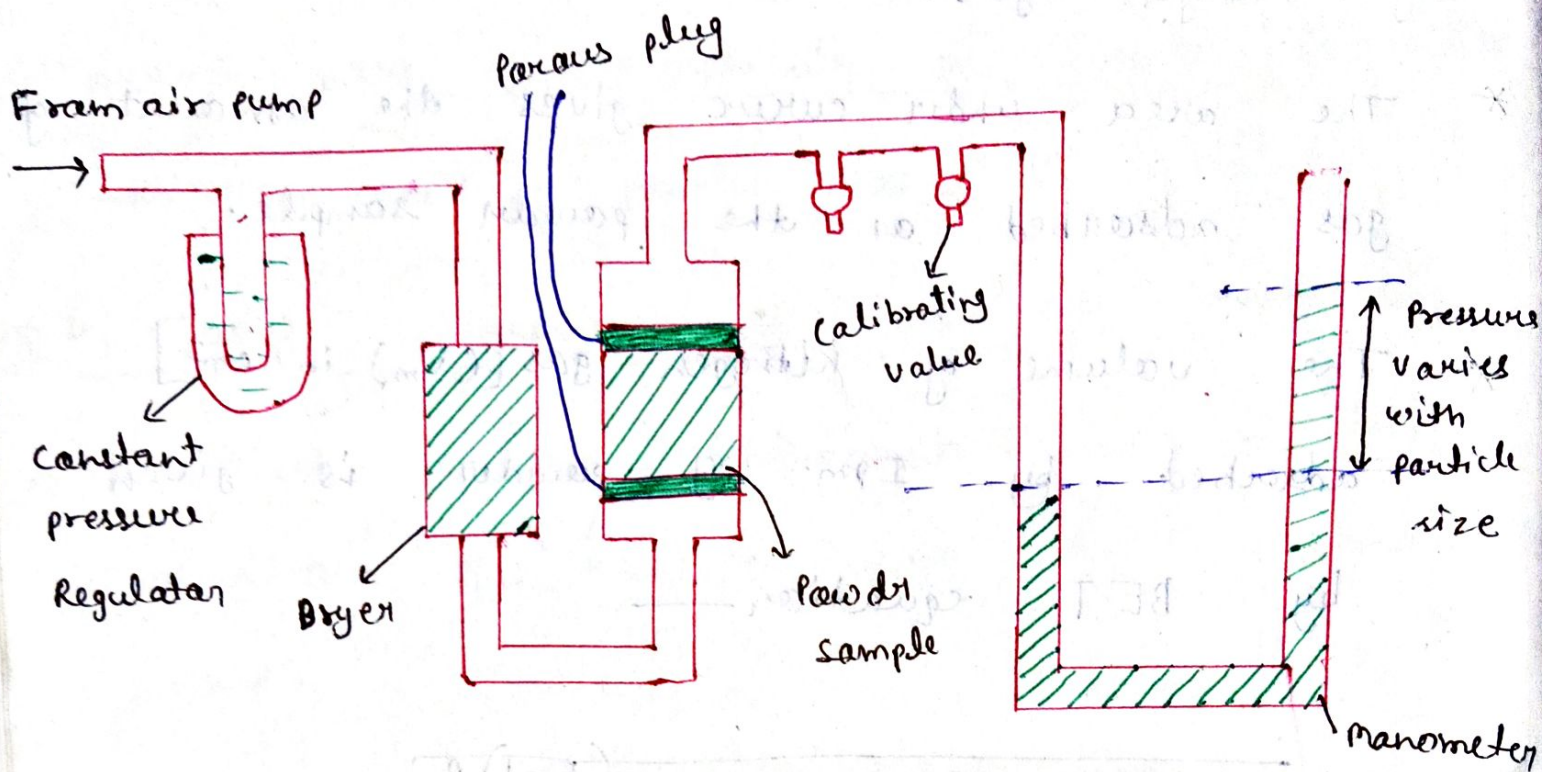
where  $\rightarrow$   $V$  = Volume of gas in  $cm^3$  adsorbed per gm. of powder at pressure  $(P)$

$P_0$  = Saturated vapour pressure of

liquid nitrogen at the temperature

$b$  = Constant.

## 2 - Air permeability method →



## Fisher sub sieve sizer

- \* It is based on the principle that the resistance offered to the flow of air through the compact powder is proportional to the surface area of the powder.
- \* The greater the surface area per gram of the powder, the greater is the resistance to flow.
- \* When the air is allowed to pass through the plug of powder resistance to the flow of air occurs.

\* This resistance is related to the surface area of the powder.

\* The specific surface ( $S_w$ ) can be calculated by Kozeny - Carman equation —

$$V = \frac{A}{\eta S_w^2} \cdot \frac{\Delta P}{k l} \cdot \frac{\epsilon^3}{(1-\epsilon)^2}$$

where →

$A$  = Cross sectional area of the plug.

$k$  = constant.

$\epsilon$  = Porosity

$V$  = Volume of air flowing.

$l$  = length of powder bed.

$\Delta P$  = Pressure difference.

### Derived properties of powder

\* A part from fundamental properties, there are derived properties which are based on funda-

-mental properties.

$$\frac{V_1 - V_2}{V}$$

\* These are as follows —

- 1- Porosity.
- 2- Packing arrangement.
- 3- Densities —————> Bulk density, tap density, granular density.
- 4- Particle volume —————> Bulk volume, tap volume, void volume.
- 5- Bulkiness.
- 6- Angle of repose.
- 7- Compaction.

1- Porosity of powder —>

Porosity is defined as the ratio of void volume to bulk volume

$$\epsilon = \frac{V_b - V_p}{V_b}$$

Porosity is expressed as percentage —

$$\% \epsilon = \frac{V_b - V_p}{V_b} \times 100$$



\* In a non-porous material, the bulk volume is equal to the true volume.

\* Most of the solids are porous that is (i.e.) they have internal pores, hence the bulk volume is greater than the true volume.

\* The volume of void space is  $\propto$  as the void volume given by  $\leftarrow$

$$V = V_b - V_p$$

where  $\rightarrow$   $V_b$  = Bulk volume

$V_p$  = True volume.

Intraparticle porosity  $\rightarrow$

It means space ~~to~~ within a single large particle.

$$\% \text{ } \epsilon = \left( 1 - \frac{\rho_g}{\rho} \right) \times 100$$

where  $\rightarrow$   $\rho_g$  = granular density

$\rho$  = True density

Inter particle porosity -

It means space b/w two

or more than two particles.

$$\% \epsilon = \left( 1 - \frac{\rho_b}{\rho} \right) \times 100$$

Where  $\rightarrow$   $\rho_b$  = Bulk density.

$\rho$  = True density.

Q-1  $\rightarrow$  True density of a given powder is

2.46 gm/cm<sup>3</sup> and 100 gm of sample occupy

bulk volume 80 cm<sup>3</sup>. Calculate % porosity.

True density = 2.46 gm/cm<sup>3</sup>

Mass = 100 gm

Bulk volume ( $V_b$ ) = 80 cm<sup>3</sup>

$$D = \frac{M}{V}$$

$$2.46 = \frac{100}{V_p}$$

$$V_p = 40.65 \text{ cm}^3$$

$$\% \epsilon = \left( \frac{V_b - V_p}{V_b} \right) \times 100$$

$$\% \epsilon = \left( \frac{80 - 40.65}{80} \right) \times 100$$

$$\% \epsilon = \frac{39.35}{80} \times 100$$

$$\% \epsilon = 49.1 \%$$

Q-2 → Calculate the intraparticle porosity of Sulfadiazine granules having a granule density of  $1.12 \text{ gm/cm}^3$  and true density of  $1.5 \text{ gm/cm}^3$ .

$$\epsilon = \left( 1 - \frac{\rho_g}{\rho} \right) \times 100$$

$$\epsilon = \left( 1 - \frac{1.12}{1.5} \right) \times 100$$

$$\epsilon = (1 - 0.74) \times 100$$

$$\epsilon = 0.26 \times 100$$

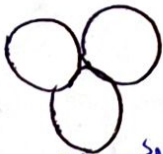
$$\epsilon = 26 \%$$

## 2-Packing arrangement in powder bed -

\* Particles of powder in a heap are constant with one another.

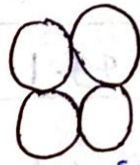
\* Two types of packing are possible theoretically these includes -

- i) closest
- ii) loosest



Theoretical closest 26%.

Practically 30%.



Theoretical loosest 48%.

Practically 50%.

\* If spherical particles are present in heap:

\* Theoretical porosity of 26% in closest & 48% in loosest packing are possible.

\* But in actual situation porosity of 30% & 50% are received.

\* If particles have different size, porosity lowers upto 26% theoretically.

\* Because particles fit in void spaces.

\* If particles contain aggregates, the porosity may go beyond 48% theoretical.

\* In case of crystalline materials porosity less than 1% are possible.

# Density -

\* Density is defined as mass per unit vol.

\* There are 3-types of densities -

- (i) True density
- (ii) Bulk density
- (iii) Granular density

(i) True Density :- It is defined as the ratio of the given mass of the powder & its volume.

It is the actual density of solid material devoid of free space.

$$\text{True Density} = \frac{\text{Mass}}{\text{True Vol.}}$$

$$\text{True volume} = \text{Bulk vol.} - \text{void vol.}$$

\* True density can be determined by -

(i) Gas-Displacement Method → In this method gas such as Helium or Hydrogen is used.

\* Difference b/w volume of Helium filling the empty apparatus & the volume of Helium filling in the presence of powder gives true volume of powder.

## ii) Liquid - displacement Method :-

- \* True density is the ratio of weight of the material & weight of the liquid it displaces
- \* A liquid in which the solid is insoluble is used.
- \* powder whose density is to be determined is added in to the flask of known volume & weight determined.
- \* The liquid fills up void spaces b/w the particles.

iii) Bulk Density  $\Rightarrow$  It is defined as the ratio of the mass of the powder & its bulk volume.

$$\text{Bulk Density} = \frac{\text{Mass}}{\text{Bulk vol.}}$$

$$\text{Bulk vol.} = \pi r^2 h$$

where

$r$  = radius of measuring cylinder

$h$  = height of powder

$\pi$  = constant (3.14)

(iii) Granular Density  $\Rightarrow$  It is the ratio of mass of the granules to the volume of the granules.

$$\text{G.D} = \frac{\text{Mass of granules}}{\text{granular vol.}}$$

\* granular density is determined by liquid displacement method by using Mercury as liquid.

## Bulkiness

- ↓ The reciprocal Bulk density is known as Bulkiness.
- ↓ Bulkiness usually increases with increase in particle size.
- ↓ In a mixture of particles with diff. sizes the bulkiness may get reduced because small particles fit b/w large ones.
- ↓ Bulkiness is useful while choosing suitable containers for packing.

## Flow property of powder

\* Powder may be free flowing or may have a poor flow.

\* The poor flow may be due to —

1- Cohesiveness or stickiness b/w particles due to vanderwall's, surface tension, electro static forces.

2- Adhesion b/w the particles and the container wall due to the above forces.

3- Friction b/w particles due to rough surface.

4- Physical interlocking of particles due to irregular shape.

\* Poor flowing powders or granules present many difficulties in pharmaceutical industries such as in tablet and capsule.

\* The flow property can be assessed by



determining the angle of repose of the powder.

$$\theta = \tan^{-1} \frac{h}{R}$$

Where  $\theta$  = Angle of repose.

$h$  = Height of heap.

$R$  = Radius of heap.

\* Angle of repose and flow property relationship are -

Angle of repose	Flow property
< 25	Excellent.
25 - 30	Good.
30 - 40	Satisfactory
40 - 50	Poor
> 50	Very poor

## Improvement of flow properties

Flow property can be improved by following methods —

1- Altering particle size —;

↑ particle size improves the flow properties due to reduction in cohesive forces.

2- Removal or addition of fines —;

An optimum concentration of fines is desirable to improve flow properties.

3- Altering the particle shape —;

Spherical particles have better flow as compared to irregular particles.

4- Removing extra moisture —;

Drying of powder can improve the flow properties by ↓ing the ~~adher~~ cohesiveness.

5- Adding glidants or flow activators -

Glidants such as talc and starch improve flow properties of powder.

Shear →

Shear can be considered as an internal friction of a fluid. caused by molecular attraction which makes it resist a tendency to flow.